

**PhD Qualifying Exam - Manufacturing  
Fall 2016**

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**Answer all problems. Clearly show all of your work. List all relevant assumptions.**

1. A solid round bar of steel has a diameter of 1 inch. When drawn to 0.57 inch in one pass using 20,000 lb of measured drawing force, the bar cracks. As an alternative to drawing, it is planned that the 1 inch bar shall be extruded to avoid cracking. If the available extruding machine offers a maximum extrusion force of 20,000 lb, what is the smallest possible final diameter in one pass of extrusion?
2. A medium carbon steel bar 100 mm in diameter is to be turned down on a lathe to 70 mm in diameter over 50 mm of its length. It is known that the specific cutting energy of the workpiece material is 2 GJ/m<sup>3</sup> and the lathe has a 3 kW spindle motor that is 80% efficient. The entire operation is divided into two consecutive steps: first, a roughing cut with 12 mm depth of cut that utilizes the maximum available power of the lathe and second, a finishing cut at a feed of 0.1 mm and an average cutting speed of 1.5 m/s. Estimate the following quantities:
  - a. The machining time required for the roughing cut.
  - b. The machining time required for the finishing cut.
  - c. The total production time for each part if the load and unload time is 20 s and it takes 30 s to set the cutting conditions, set the tool at the beginning of each cut, and engage the feed.
  - d. The average cutting forces generated in the roughing and finishing cuts. Assume the feed in the roughing cut to be the same as specified above for the finishing cut.
  - e. Briefly discuss at least two ways by which you can reduce the cutting force in the roughing operation without compromising the productivity of the operation.
3. An extruder has a barrel diameter of 75 mm and rotates at 100 rpm. The screw has a channel depth of 6 mm, a channel width of 35 mm, and a flight angle of 17.5 degrees. The pumping section of the screw is 3 m long and is used to extrude a rod polyethylene rod. When melted, the polyethylene has a viscosity of 80 N-s/m<sup>2</sup>. The die has a diameter of 5 mm and is 10 mm long.
  - a. Determine the flow rate through the die.
  - b. With the aid of a graph of the specific volume versus temperature, explain the importance of the injection pressure or extrusion pressure during polymer processing.

Die flow equations based on geometry

**Rectangular**  $Q = \frac{wH^3}{12\mu} \frac{\Delta p}{L}$

**Cylindrical**  $Q = \frac{\pi R^4}{8\mu} \frac{\Delta p}{L}$

### Screw flow equation

$$Q = w \left[ \frac{v_z H}{2} - \frac{H^3}{12\mu} \frac{dp}{dz} \right]$$

### Nomenclature:

Q = flow rate (m<sup>3</sup>/s)

w = width of flight or channel (m)

H = height of flight or channel (m)

μ = viscosity (N-s/m<sup>2</sup>)

R = radius of channel (m)

L = dz = length of channel (m)

Δp or dp = pressure drop or back pressure (Pa)

v<sub>z</sub> = velocity along flight (helix)

z = direction along flight (helix)

ρ = density

r = radius